

# Public Key Infrastructure

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## Question in Public key

- How can Bob believe that Alice's public key is real?
- Bob obtains Alice's public key from any other sources than Alice herself. Then how can he trust that it is really her public key?

# Public Key Certificate

- **Certificate** contains name of user and user's public key (and possibly other info)
- Any trusted issuer, called a ***Certificate Authority (CA)***, issues the Alice's certificate after she registers her public key to the CA,

$M = (\text{Alice}, \text{Alice's public key})$

CA guarantees the certificate by signing the certificate using its private key:

$$s = \text{sign}_{K\text{-CA}}(M)$$

**Alice's Certificate** =  $(M, S)$

# Certificate Authority

- ❑ Certificate authority (CA) is a trusted third party (TTP) — creates and signs certificates
- ❑ Verifying signature proves the integrity & identity of **the user's public key** to which the certificate refers.
  - Does **not** verify the identity of the publisher of the certificate.
- ❑ Big problem if CA makes a mistake.
- ❑ A common standard format for certificates is **X.509**.

## X.509 certificate example(1)

- Next slide is a certificate to verify the public key of [www.freesoft.org](http://www.freesoft.org).
- CA is **Thawte**.
- Thawte signed at the bottom of the certificate to verify the certificate. (signature)
- The recipient can verify this certificate by confirming the signature by using Thawte's public key.
- Then he can trust the freesoft's public key in the certificate.

Certificate:

Data:

Version: 1 (0x0)  
Serial Number: 7829 (0x1e95)  
Signature Algorithm: md5WithRSAEncryption  
Issuer: C=ZA, ST=Western Cape, L=Cape Town, O=Thawte Consulting cc,  
OU=Certification Services Division,  
CN=Thawte Server CA/emailAddress=server-certs@thawte.com

Validity

Not Before: Jul 9 16:04:02 1998 GMT

Not After : Jul 9 16:04:02 1999 GMT

Subject: C=US, ST=Maryland, L=Pasadena, O=Brent Baccala,  
OU=FreeSoft, CN=www.freesoft.org/emailAddress=baccala@freesoft.org

Subject Public Key Info:

Public Key Algorithm: rsaEncryption

RSA Public Key: (1024 bit)

Modulus (1024 bit):

00:b4:31:98:0a:c4:bc:62:c1:88:aa:dc:b0:c8:bb:  
33:35:19:d5:0c:64:b9:3d:41:b2:96:fc:f3:31:e1:  
66:36:d0:8e:56:12:44:ba:75:eb:e8:1c:9c:5b:66:  
70:33:52:14:c9:ec:4f:91:51:70:39:de:53:85:17:  
16:94:6e:ee:f4:d5:6f:d5:ca:b3:47:5e:1b:0c:7b:  
c5:cc:2b:6b:c1:90:c3:16:31:0d:bf:7a:c7:47:77:  
8f:a0:21:c7:4c:d0:16:65:00:c1:0f:d7:b8:80:e3:  
d2:75:6b:c1:ea:9e:5c:5c:ea:7d:c1:a1:10:bc:b8:  
e8:35:1c:9e:27:52:7e:41:8f

Exponent: 65537 (0x10001)

Signature Algorithm: md5WithRSAEncryption

93:5f:8f:5f:c5:af:bf:0a:ab:a5:6d:fb:24:5f:b6:59:5d:9d:  
92:2e:4a:1b:8b:ac:7d:99:17:5d:cd:19:f6:ad:ef:63:2f:92:  
ab:2f:4b:cf:0a:13:90:ee:2c:0e:43:03:be:f6:ea:8e:9c:67:  
d0:a2:40:03:f7:ef:6a:15:09:79:a9:46:ed:b7:16:1b:41:72:  
0d:19:aa:ad:dd:9a:df:ab:97:50:65:f5:5e:85:a6:ef:19:d1:  
5a:de:9d:ea:63:cd:cb:cc:6d:5d:01:85:b5:6d:c8:f3:d9:f7:  
8f:0e:fc:ba:1f:34:e9:96:6e:6c:cf:f2:ef:9b:bf:de:b5:22:  
68:9f

## X.509 certificate example(2)

- Then, how can the recipient know the Thawte's public key?
- Thawte lets the recipient know its public key through another certificate which is signed by its private key.
- Next slide is the certificate through which Thawte releases its public key.



Certificate:

Data:

Version: 3 (0x2)  
Serial Number: 1 (0x1)  
Signature Algorithm: md5WithRSAEncryption  
Issuer: C=ZA, ST=Western Cape, L=Cape Town, O=Thawte Consulting cc,  
OU=Certification Services Division,  
CN=Thawte Server CA/emailAddress=server-certs@thawte.com

Validity

Not Before: Aug 1 00:00:00 1996 GMT

Not After : Dec 31 23:59:59 2020 GMT

Subject: C=ZA, ST=Western Cape, L=Cape Town, O=Thawte Consulting cc,  
OU=Certification Services Division,  
CN=Thawte Server CA/emailAddress=server-certs@thawte.com

Subject Public Key Info:

Public Key Algorithm: rsaEncryption

RSA Public Key: (1024 bit)

Modulus (1024 bit):

00:d3:a4:50:6e:c8:ff:56:6b:e6:cf:5d:b6:ea:0c:  
68:75:47:a2:aa:c2:da:84:25:fc:a8:f4:47:51:da:  
85:b5:20:74:94:86:1e:0f:75:c9:e9:08:61:f5:06:  
6d:30:6e:15:19:02:e9:52:c0:62:db:4d:99:9e:e2:  
6a:0c:44:38:cd:fe:be:e3:64:09:70:c5:fe:b1:6b:  
29:b6:2f:49:c8:3b:d4:27:04:25:10:97:2f:e7:90:  
6d:c0:28:42:99:d7:4c:43:de:c3:f5:21:6d:54:9f:  
5d:c3:58:e1:c0:e4:d9:5b:b0:b8:dc:b4:7b:df:36:  
3a:c2:b5:66:22:12:d6:87:0d

Exponent: 65537 (0x10001)

X509v3 extensions:

X509v3 Basic Constraints: critical

CA:TRUE

Signature Algorithm: md5WithRSAEncryption

07:fa:4c:69:5c:fb:95:cc:46:ee:85:83:4d:21:30:8e:ca:d9:  
a8:6f:49:1a:e6:da:51:e3:60:70:6c:84:61:11:a1:1a:c8:48:  
3e:59:43:7d:4f:95:3d:a1:8b:b7:0b:62:98:7a:75:8a:dd:88:  
4e:4e:9e:40:db:a8:cc:32:74:b9:6f:0d:c6:e3:b3:44:0b:d9:  
8a:6f:9a:29:9b:99:18:28:3b:d1:e3:40:28:9a:5a:3c:d5:b5:  
e7:20:1b:8b:ca:a4:ab:8d:e9:51:d9:e2:4c:2c:59:a9:da:b9:  
b2:75:1b:f6:42:f2:ef:c7:f2:18:f9:89:bc:a3:ff:8a:23:2e:  
70:47

## X.509 certificate example(3)

- Then, how can the recipient trust this certificate? In other words, how can he believe that Thawte is a trusted CA?
- Then, he needs another CA which can verify the Thawte's certificate(its public key).
- This situation raises the chain of trust.
- So, there should be a root CA (or CAs) at the top of all CAs (if we use the hierarchical structure of CAs).

# PKI

- ❑ **Public Key Infrastructure (PKI)** is needed to securely use public key crypto by specifying the following:
  - Key generation and management
  - Certificate authority (CA) or authorities
  - Certificate revocation lists (CRLs), etc.
- ❑ No general standard structure for PKI
- ❑ For instance, multiple trusted CAs are used in web browsers today.